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# B.Sc. DEGREE EXAMINATION, May 2015 <br> (MATHEMATICS WITH COMPUTER APPLICATIONS) <br> (THIRD YEAR) <br> (PART - III) 

## 720: MATHEM ATICAL STATISTICS

Time: Three hours
Maximum: 100 marks

## Answer any FIVE Full questions

$(5 \times 20=100)$

1. a) State and prove addition Theorem on probabilities.
b) State and prove Multiplication theorem on probabilities.
c) State and prove Baye's theorem.
d) A random variables ' $x$ ' has the following probability distribution.

| X | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{P}(\mathrm{x})$ | a | 3 a | 5 a | 7 a | 9 a | 11 a | 13 a | 15 a | 17 a |

i) Find the value of (a)
ii) Find $\mathrm{p}(\mathrm{x}<3), \mathrm{p}(\mathrm{x} \geq 3)$
2. a) Fit a straight line to the following data.

| X | 1 | 2 | 3 | 4 | 6 | 8 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Y | 2.4 | 3 | 3.6 | 4 | 5 | 6 |

b) Describe the method of fitting the following curves.
i) $Y=a e^{b x}$
ii) $Y=a x^{b}$
$\begin{array}{lllllllllll}3 . & \text { a) } & \mathrm{X}: & 14 & 19 & 24 & 21 & 26 & 22 & 15 & 20 \\ \mathrm{Y} & \text { : } & 31 & 36 & 48 & 37 & 50 & 45 & 33 & 41 & 39\end{array}$ Calculate the correlation co-efficient between the x and y .
b) Define rank correlation and derive $r=1-\frac{6 \Sigma d^{2}}{n\left(n^{2}-1\right)}$
4. a) State chief characteristics of normal distribution
b) Show that the rectangular distribution.
$f(x)=\frac{1}{2 a}-a<x<a$ the m.g.f about origin is $\frac{1}{a t}$ (sinhat). Also show that moments of even order are given by $\mu 2 \mathrm{n}=\frac{a^{2 n}}{(2 n+1)}$
5. a) Explain the test procedure to list the population proportion.
b) Derive the student's t-distribution.
c) In one sample of 8 observations, the sum of the squares of deviations of the sample values form the sample mean was 84.4 and in the other sample of 10 observations it was 102.6. Test wheather this difference is significant at $5 \%$ level, given that $5 \%$ point of for $\mathrm{n}_{1}=7$ and $\mathrm{n}_{2}=9$ dof if 3-29.
6. a) Explain methods of Estimation.
b) From the following table, estimate the number of students who obtained marks b/w 40 and 45.

| Marks | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| No. of students | 31 | 42 | 51 | 35 | 31 |

7. a) Setup an analysis of variance table for one-way classification.
b) Show that fisher's ideal index satisfies both T.R. and F.R tests, using the following data commonly.

|  | $\mathbf{1 9 9 0}$ |  | $\mathbf{1 9 9 2}$ |  |
| :---: | :---: | :---: | :---: | :---: |
| Commodity | $\mathbf{P}$ | $\mathbf{Q}$ | $\mathbf{P}$ | $\mathbf{Q}$ |
| $\mathbf{A}$ | 6 | 50 | 10 | 56 |
| $\mathbf{B}$ | 2 | 100 | 2 | 120 |
| $\mathbf{C}$ | 4 | 60 | 6 | 60 |
| $\mathbf{D}$ | 10 | 30 | 12 | 24 |
| $\mathbf{E}$ | 8 | 40 | 12 | 36 |

8. a) Explain : i) Secular trend
ii) Seasonal variations
iii) cyclical Fluctuations
b) Sate and derive Lagrange's interpolation formula.
9. a) Interpolate Y when $\mathrm{x}=12$.

| $\mathbf{X}$ | 10 | 15 | 25 |
| :--- | :---: | :---: | :---: |
| $\mathbf{Y}$ | 90 | 215 | 615 |

b) Interpolate the value of $Y$ when $x=0$ using Lagrange's formula:

| $\mathbf{X}$ | -1 | -2 | 2 | 4 |
| :--- | :---: | :---: | :---: | :---: |
| $\mathbf{Y}$ | -1 | -9 | 11 | 69 |

10. a) For a normal distribution prove that
Q:D;M,D;S;D::10:12:15
b) Explain non-random sampling.
