Register Number:
Name of the Candidate:

# B.Sc. DEGREE EXAMINATION, May 2015 <br> (MATHEMATICS WITH COMPUTER APPLICATIONS) <br> (SECOND YEAR) <br> (PART - III) 

## 640: OPERATIONS RESEARCH

Time: Three hours
Maximum: 100 marks

## Answer any FIVE Full questions

1. a) Explain the advantages of LPP.
b) A firm manufactures two products A and B on which the profits earned per unit are ₹3 and ₹4 respectively. Each product is processed on two machines M1 and M2. Product A requires one minute of processing time on M1 and two minutes on M2 while B requires one minute on M1 and 5minutes on M2. Machine M1 is available for not more than 7 hours 30 minutes while machine M2 is available only for 10 hours during any working day. Find the number of units of products A and B to be manufactured to get maximum profit. Formulate the above as a LPP and solve by Graphical method.
2. Use simplex method to

$$
\begin{array}{cl}
\text { Minimize } & Z=x_{2}-3 x_{3}+2 x_{5} \\
\text { Sub to: } & 3 x_{2}-x_{3}+2 x_{5} \leq 7 \\
& -2 x_{2}+4 x_{3} \leq 12 \\
& -4 x_{2}+3 x_{3}+8 x_{5} \leq 10 \text { and } \\
& x_{2}, x_{3}, x_{5} \geq 0
\end{array}
$$

3. a) Using simplex algorithm.

Minimize $Z=-2 x_{1}-x_{2}$
Sub to : $\quad \mathrm{x}_{1}+\mathrm{x}_{2} \geq 2$
$\mathrm{x}_{1}+\mathrm{x}_{2} \leq 4$
$\mathrm{x}_{1}, \mathrm{x}_{2} \geq 0$
b) Write down the disadvantage of Big M method over Two - phase method.
4. Using dual simplex method solve the LPP.

$$
\begin{array}{ll}
\text { Maximize } & Z=2 x_{1}+3 x_{2} \\
\text { Sub to : } & 2 x_{1}-x_{2}-x_{3} \geq 3 \\
& x_{1}-x_{2}+x_{3} \geq 2 \text { and } x_{1}, x_{2}, x_{3} \geq 0
\end{array}
$$

5. a) Solve the transportation problem by modified distribution method.

|  | 1 | 2 | 3 | 4 | Supply <br> 11 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| I | 21 | 16 | 25 | 13 |  |
| II | 17 | 18 | 14 | 23 | 13 |
| III | 32 | 27 | 18 | 41 | 19 |
| emand | 6 | 10 | 12 | 15 |  |

6. a) Distinguish between Transportation model and Assignment model.
b) Solve the assignment problem for maximization of profit matrix (Profit given below are in rupees).

Machines

|  |  | P | Q | R | S |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | A | 51 | 53 | 54 | 50 |
|  | B | 47 | 50 | 48 | 50 |
|  | C | 49 | 50 | 60 | 61 |
|  | D | 63 | 64 | 60 | 60 |

7. a) What is a sequencing problem?
b) State the Principal assumptions made while dealing with sequencing problem.
c) Explain the seque ncing problem of ' $n$ ' jobs on ' $m$ ' machines.
8. a) Prove that dual of the dual is primal.
b) Explain inventory models.
9. a) A machine owner finds from his past records that the cost per year of maintaining a machine purchase price ₹6,000 are as given below.

| Year | $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{c}$ | $\mathbf{4}$ | $\mathbf{5}$ |
| :--- | :---: | :---: | ---: | ---: | ---: | ---: |
| $\mathbf{c}$ | $\mathbf{6}$ |  |  |  |  |  |
| Maintenance cost $(₹)$ | 1000 | 1200 | 1400 | 1800 | 2300 | 2800 |
| Resale value $(₹)$ | 3000 | 1500 | 750 | 375 | 200 | 200 |

Determine at what age replacement need to be done.
b) Explain replacement problem

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a) Explain EOQ.
b) Solve the sequencing problem

|  | J1 | J2 | J3 | J4 | J5 | J6 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| M1 | 4 | 13 | 6 | 3 | 10 | 12 |
| M2 | 9 | 7 | 5 | 7 | 4 | 2 |
| M3 | 13 | 15 | 10 | 13 | 9 | 14 |
|  |  |  |  |  |  | $\$ \$ \$ \$ \$$ |

